

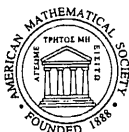
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Centre de Recherches Mathématiques
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Moduli Spaces and Arithmetic Dynamics

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